

Quantum Dynamics with a Smolyak scheme. Applications to clathrate hydrates.

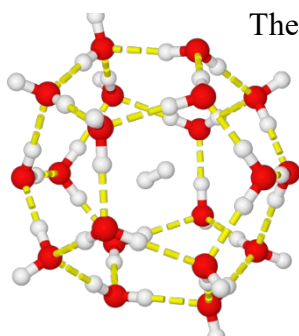
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The use of Smolyak scheme in quantum dynamics is an approach that pushes the limits of the current calculations based on a multidimensional basis set and grid. More precisely, the Smolyak scheme^{a-c} can be viewed as an approach involving a selection of basis functions and a sparse grid adapted to that basis set. The parameter, L , controls the selection and thus the size of the basis set and grid. With this scheme, the numerical complexity grows as a polynomial of degree L with respect to the number of degrees of freedom d . Systems with up to 12 degrees of freedom can be studied,^{d-f} although larger systems ($d=21$) are possible if few states are needed.^g This limit can be pushed away using a system-bath separation, and in our Smolyak scheme.^h



The spectroscopy studies (neutron, Raman ...) of encapsulated molecules in cages such as clathrates hydrates (see figure on the left), fullerenes, enable precise characterization of these systems.ⁱ⁻¹ In particular, vibrational shifts and/or translation/rotation motions of the encapsulated molecule provide information about the interactions between the encapsulated molecule and the cage. Results for H₂ or CO encapsulated in rigid or flexible cages will show the efficiency of this sparse grid technique.^{m,h}

References:

- ^a Smolyak, S. A. Soviet Mathematics Doklady 1963, 4, 240. <https://www.mathnet.ru/eng/dan27586>
- ^b Avila, G.; Carrington, T. JCP 2009, 131, 174103. <https://doi.org/10.1063/1.3246593>
- ^c Lauvergnat, D.; Nauts, A. PCCP 2010, 12, 8405–12. <https://doi.org/10.1039/C001944E>
- ^d Lauvergnat, D.; Nauts, A.; Spectrochimica Acta Part A: 2014, 119, 18–25. <https://doi.org/10.1016/j.saa.2013.05.068>
- ^e Avila, G.; Carrington, T. JCP 2017, 147, 064103. <https://doi.org/10.1063/1.4994920>
- ^f Avila, G.; Mátyus, E. JCP 2019, 150, 174107. <https://doi.org/10.1063/1.5090846>
- ^g Lauvergnat, D.; Nauts, A.; ChemPhysChem, 2023, 24, 202300501. <https://doi.org/10.1002/cphc.202300501>
- ^h Chen, A.; Benoit, D. M.; Scribano, Y.; Nauts, A.; Lauvergnat, D. JCTC 2022, 18, 4366–4372. <https://doi.org/10.1021/acs.jctc.2c00108>
- ⁱ Ulivi, L. et al., Phys. Rev. B 2007, 76, 161401. <https://doi.org/10.1103/PhysRevB.76.161401>
- ^j Strobel, T. A. et al. CPL 2009, 478, 97–109. <https://doi.org/10.1016/j.cplett.2009.07.030>
- ^k Xu, M.; Sebastianelli, F.; Bačić, Z. JCP 2008, 128, 244715. <https://doi.org/10.1063/1.2945895>
- ^l Valdés, Á.; Prosimi, R. JCP, 2024, 160, 184304. <https://doi.org/10.1063/5.0210866>
- ^m Lauvergnat, D.; Felker, P.; Scribano, Y.; Benoit, D. M.; Bačić, Z. JCP 2019, 150, 154303. <https://doi.org/10.1063/1.5090573>